# **Motion**<sup>®</sup>

# SAMPLE PAPER – JEE MAIN

Duration: 3 Hours

Max. Marks : 300

#### INSTRUCTIONS

In each part of the paper contains **30** questions. Please ensure that the Questions paper you have received contains <u>ALL THE QUESTIONS</u> in each Part.

In each Part of The paper Section A Contain 20 Questions. Each Question has four choices (A), (B), (C), (D) out of which only one is correct & carry 4 marks each. 1 mark will be deducted for each wrong answer.

In each Part of The paper Section B Contains 10 Numeric Value type questions. Candidates have to attempt any 5 Ques. out of 10. For each question, enter the correct numerical value ((If the numerical value has more than two decimal places, truncate/ round-off the value to TWO decimal places; e.g. 6.25, 7.00, 0.33, 30.27, 127.30.)

Each Question Carry  $4\ Marks$  & No Negative marking in these Section.

#### NOTE : GENERAL INSTRUCTION FOR FILLING THE OMR ARE GIVEN BELOW.

- 1. Use only **blue/black pen (avoid gel pen)** for darkening the bubble.
- **2.** Indicate the correct answer for each question by filling appropriate bubble in your OMR answer sheet.
- **3.** The Answer sheet will be checked through computer hence, the answer of the question must be marked by shading the circles against the question by dark **blue/black pen**.
- **4.** Blank papers, Clipboards, Log tables, Slide Rule, Calculators, Cellular Phones, Pagers and Electronic Gadgets in any form are **not** allowed to be carried inside the examination hall.

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#### PART - I [MATHEMATICS]

#### **SECTION - A**

#### [STRAIGHT OBJECTIVE TYPE]

- Q.1 to Q.20 has four choices (A), (B), (C), (D) out of which ONLY ONE is correct
- Number of ways of selection of 4 letters of the word " PERFECT" is

   (A) 15
   (B) 21
  - (C) 25 (D) 31
- 2. A pole 50m high on a building 250m high. An observer at a height of 300m from ground the building and pole subtend equal angle 0. If horizontal distance of observer and pole is 'x'. Then

(A)  $x = 25\sqrt{3}m$  (B)  $x = 25\sqrt{6}m$ (C)  $x = 5\sqrt{3}m$  (D)  $x = 5\sqrt{6}m$ 

- **3.** The negation of the compound proposition  $p_{\vee}$  (~  $p_{\vee}$  q) is
  - (A)  $(p \land \sim q) \land \sim p$  (B)  $(p \land \sim q) \lor \sim p$
  - (C)  $(p \lor \sim q) \lor \sim p$  (D) None of these

- 4. If  $A^3 = 0$  then I+A+  $A^2$  equals:-(A) I-A (B) (I-A)^{-1} (C) (I+A)^{-1} (D) I
- 5. If  $x^2 + y^2 + z^2 = 1$ , where x, y,  $z \in R^+$ then greatest value of  $x^2y^3z^4$  is

(A) 
$$\frac{2^5}{3^{15/2}}$$
 (B)  $\frac{2^{10}}{3^{15}}$  (C)  $\frac{2^{10}}{3^{9/2}}$  (D)  $\frac{2^{12}}{3^9}$ 

6. A coin is tossed 7 times, Then probability that at least 4 consecutive heads appear is :

(A) 
$$\frac{3}{16}$$
 (B)  $\frac{5}{32}$  (C)  $\frac{1}{8}$  (D)  $\frac{1}{4}$ 

- 7. If  $p,q,r,s \in R$  then equation :  $(x^2 + px + 3q)(-x^2 + rx + q)$   $(-x^2 + sx - 2q) = 0$  has (A) 6 real roots (B) at least two real roots (C) 2 real and 4 imaginary roots
  - (D) 4 real & 2 Imaginary roots

#### (SPACE FOR ROUGH WORK)

$(\tan^{-1}x)(\cot^{-1}x) = (\tan^{-1}x)\left(1+\frac{\pi}{2}\right) - 2\cot^{-1}x$ $+ 2\left(1+\frac{\pi}{2}\right) > \lim_{x \to \infty} \left[\sec^{-1}x - \frac{\pi}{2}\right] \text{ is (where function)}$ (A) (tan1, tan2) (B) (-cot1, cot2) (C) (-tan1, tan2) (D) (-tan1, \infty) 9. If $w = \frac{z - (1/5)i}{z}$ and $ w  = 1$ , then complex number z lies on (A) a parabola (B) a circle (C) a line (D) none of these (C) a line (D) none of these (C) a line (D) none of these (A) 5 (B) 6 (C) 7 (D) 8 11. Let $f(x) = \begin{cases} \frac{\sin ax^2}{x^2}; x \neq 0\\ \frac{3}{4} + \frac{1}{4a}; x = 0\\ for what values of a, f(x) is continuous at x = 0: (A) 1, -1/4 (B) 1, 0 (A) 1, -1/4 (B) 1, 0 (A) (A) (A) (A) (A) (A) (A) (A) (A) (A)$	8.	The solution set of inequality	12.	If $f(x) = \frac{10^x - 10^{-x}}{10^{-x}} + 2$ ; then $f^{-1}(y) = ?$
[.] denotes the greatest integer function) (A) (tan1, tan2) (B) (-cot1, cot2) (C) (-tan1, tan2) (D) (-tan1, $\infty$ ) 9. If $w = \frac{z - (1/5)i}{z}$ and $ w  = 1$ , then complex number z lies on (A) a parabola (B) a circle (C) a line (D) none of these 10. $(x + \sqrt{x^3 - 1})^5 + (x - \sqrt{x^3 - 1})^5$ is a polynomial of the order of - (A) 5 (B) 6 (C) 7 (D) 8 11. Let $f(x) =\begin{cases} \frac{\sin ax^2}{x^2}; x \neq 0\\ \frac{3}{4} + \frac{1}{4a}; x = 0\end{cases}$ for what values of a, $f(x)$ is continuous at $x = 0$ : (A) $1, -1/4$ (B) $1, 0$ (C) $\frac{1}{2} \log_{10}(\frac{3}{3-y})$ (D) $\frac{1}{2} \log_{10}(\frac{1}{y})$ 13. If $f(x) = \begin{vmatrix} x^2 + 3x + x - 1 + x - 3\\ x + 1 - 2 - x + x - 3\\ x - 3 + 4 - 3x \end{vmatrix}$ , then f'(0) is equal to (A) - 39 (B) 64 (C) 24 (D) 52 14. $\lim_{n \to \infty} \left\{ \frac{1}{(n+1)(n+2)} + \frac{1}{(n+2)(n+4)} + \dots + \frac{1}{6n^2} \right\}$ = (A) $\log (3/2)$ (B) $\log (2/3)$ (C) $\frac{1}{3} \log 2$ (D) $\frac{1}{2} \log 3$ 15. The area bounded by the loop of the curve $4y^2 = x^2(4 - x^2)$ is (A) 7/3 sq. units (B) 8/3 sq. units (C) 11/3 sq. units (D) 16/3 sq. units		$(\tan^{-1}x)(\cot^{-1}x) - (\tan^{-1}x)\left(1+\frac{\pi}{2}\right) -2\cot^{-1}x$ $+ 2\left(1+\frac{\pi}{2}\right) > \lim_{x\to\infty}\left[\sec^{-1}x-\frac{\pi}{2}\right] \text{ is (where }$		$(A) \frac{1}{2} \log_{10} \left( \frac{y-1}{y-3} \right) \qquad (B) \frac{1}{2} \log_{10} \left( \frac{y-3}{y-1} \right)$ $(C) \frac{1}{2} \log_{10} \left( \frac{y-1}{y-3} \right) \qquad (D) \frac{1}{2} \log_{10} \left( \frac{y-1}{y-1} \right)$
9. If $w = \frac{z - (1/5)i}{z}$ and $ w  = 1$ , then complex number z lies on (A) a parabola (B) a circle (C) a line (D) none of these 10. $(x + \sqrt{x^3 - 1})^5 + (x - \sqrt{x^3 - 1})^5$ is a polynomial of the order of - (A) 5 (B) 6 (C) 7 (D) 8 11. Let $f(x) = \begin{cases} \frac{\sin ax^2}{x^2}; x \neq 0\\ \frac{3}{4} + \frac{1}{4a}; x = 0 \end{cases}$ for what values of a, $f(x)$ is continuous at $x = 0$ : (A) $1, -1/4$ (B) $1, 0$ (C) $\frac{1}{3}$ sq. units (B) $\frac{3}{4}$ sq. units (A) $\frac{1}{2}$ log3 (C) $\frac{1}{3}$ log2 (D) $\frac{1}{2}$ log3 (C) $\frac{1}{3}$ log2 (D) $\frac{1}{2}$ log3 (C) $\frac{1}{3}$ log2 (D) $\frac{1}{2}$ log3 (C) $\frac{1}{3}$ sq. units (B) $\frac{8}{3}$ sq. units (A) $\frac{7}{3}$ sq. units (B) $\frac{8}{3}$ sq. units (C) $\frac{11}{3}$ sq. units (D) $\frac{16}{3}$ sq. units		[.] denotes the greatest integer function) (A) (tan1, tan2) (B) (-cot1, cot2) (C) (-tan1, tan2) (D) (-tan1, $\infty$ )	12	$(C) \frac{1}{2} \log_{10} \left( \frac{1}{3 - y} \right)  (D) \frac{1}{2} \log_{10} \left( \frac{1}{y} \right)$ If $f(x) = \begin{vmatrix} x^2 + 3x & x - 1 & x - 3 \\ x + 1 & 2 - x & x - 3 \end{vmatrix}$
<b>10.</b> $(x + \sqrt{x^3 - 1})^5 + (x - \sqrt{x^3 - 1})^5$ is a polynomial of the order of - (A) 5 (B) 6 (C) 7 (D) 8 <b>14.</b> $\lim_{n \to \infty} \left\{ \frac{1}{(n+1)(n+2)} + \frac{1}{(n+2)(n+4)} + \dots + \frac{1}{6n^2} \right\}$ = (A) log (3/2) (B) log (2/3) (C) $\frac{1}{3} \log 2$ (D) $\frac{1}{2} \log 3$ <b>15.</b> The area bounded by the loop of the curve $4y^2 = x^2(4 - x^2)$ is (A) 7/3 sq. units (B) 8/3 sq. units (C) 11/3 sq. units (D) 16/3 sq. units	9.	If $w = \frac{z - (1/5)i}{z}$ and $ w  = 1$ , then complex number z lies on (A) a parabola (B) a circle (C) a line (D) none of these	13.	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
11. Let $f(x) = \begin{cases} \frac{\sin ax^2}{x^2}; x \neq 0 \\ \frac{3}{4} + \frac{1}{4a}; x = 0 \end{cases}$ for what values of a, $f(x)$ is continuous at $x = 0$ : (A) 1, -1/4 (B) 1, 0 (C) $\frac{1}{3} \log 2$ (D) $\frac{1}{2} \log 3$ 15. The area bounded by the loop of the curve $4y^2 = x^2(4 - x^2)$ is (A) 7/3 sq. units (B) 8/3 sq. units (C) $\frac{1}{3} \log 2$ (D) $\frac{1}{2} \log 3$	10.	$(x + \sqrt{x^3 - 1})^5 + (x - \sqrt{x^3 - 1})^5$ is a polynomial of the order of - (A) 5 (B) 6 (C) 7 (D) 8	14.	$\lim_{n \to \infty} n \left\{ \frac{1}{(n+1)(n+2)} + \frac{1}{(n+2)(n+4)} + \dots + \frac{1}{6n^2} \right\}$ = (A) log (3/2) (B) log (2/3)
(C) 1/4, 1 (D) None (C) 11/5 5q. amos (D) 10/5 5q. amos	11.	Let $f(x) = \begin{cases} \frac{\sin ax^2}{x^2}; & x \neq 0 \\ \frac{3}{4} + \frac{1}{4a}; & x = 0 \end{cases}$ for what values of a, f(x) is continuous at x = 0: (A) 1, -1/4 (B) 1, 0 (C) 1/4, 1 (D) None	15.	(C) $\frac{1}{3}\log 2$ (D) $\frac{1}{2}\log 3$ The area bounded by the loop of the curve $4y^2 = x^2(4 - x^2)$ is (A) 7/3 sq. units (B) 8/3 sq. units (C) 11/3 sq. units (D) 16/3 sq. units

(SPACE FOR ROUGH WORK)

- 16. Equation of the curve satisfying  $xdy - ydx = \sqrt{x^2 - y^2} dx; y(1) = 0 is :-$ (A)  $y = x^2 sin(logx)$  (B)  $y^2 = x (x - 1)^2$ (C)  $y^2 = x^2(x - 1)$  (D) y = xsin(logx)
- **17.** Let  $\alpha_0$ ,  $\alpha_1$ ,  $\alpha_2$ , .....,  $\alpha_{n-1}$  be the n distinct n<sup>th</sup> roots of the unity, then the value of  $\sum_{r=0}^{n-1} \frac{\alpha_r}{3-\alpha_r}$  is equal to (A)  $\frac{n}{3^n-1}$  (B)  $\frac{n-1}{3^n-1}$ (C)  $\frac{n+1}{3^n-1}$  (D)  $\frac{n+2}{3^n-1}$
- **18.** A pole inclined from vertical at  $15^{\circ}$  towards the sun. Length of the shadow of the pole is  $\sqrt{3} + 1$  meter at the time when angle of elevation of the sun is  $30^{\circ}$ , then length of pole is

(A) 
$$\frac{\sqrt{3}-1}{\sqrt{2}}$$
 m (B)  $\frac{\sqrt{2}}{\sqrt{3}-1}$  m  
(C)  $\frac{\sqrt{3}+1}{\sqrt{3}-1}$  m (D)  $\frac{1}{\sqrt{2}}$  m

- **19.** Let  $\alpha \in \mathbb{R}$  and the three vectors ,  $\vec{a} = \alpha \hat{i} + \hat{j} + 3\hat{k}$   $\vec{b} = 2\hat{i} + \hat{j} - \alpha \hat{k}$  and  $\vec{c} = \alpha \hat{i} - 2\hat{j} + 3\hat{k}$ . Then the set  $S = \{\alpha : \hat{a}, \hat{b} \text{ and } \hat{c} \text{ are coplanar} \}$ (A) is singleton (B) Contains exactly two numbers only one of which of positive (C) Contains exactly two positive numbers (D) is empty
- **20.** The length of the perpendicular drawn from the point (2, 1, 4) to the plane containing the lines

$$\vec{r} = (\hat{i} + \hat{j}) + \lambda (\hat{i} + 2\hat{j} - \hat{k})$$
  
and  $\vec{r} = (\hat{i} + \hat{j}) + \mu (-\hat{i} + \hat{j} - 2\hat{k})$  is:  
(A)  $\sqrt{3}$  (B)  $\frac{1}{\sqrt{3}}$ 

(C) 
$$\frac{1}{3}$$
 (D) 3

#### SECTION - B

#### [NUMERICAL VALUE TYPE]

*Q.1* to *Q.10* are NUMERIC VALUE TYPEQuestions. Candidates have to attempt any5 Ques. out of 10.

#### (SPACE FOR ROUGH WORK)

- How many ways 5 balls can be placed in 3 boxes such that no box remains empty if balls as well as boxes are identical ?
- 2. Let  $f:(-3, 3) \rightarrow R$  be a differentiable function with f(0) = -2, and f'(0) = -1and  $g(x) = (f(3f(x) + 6))^3$ . then g'(0) is equal to .
- **3.** At present a firm is manufacturing 2000 items. It is estimated that the rate of change of production P w.r.t. additional number of workers x is given by  $\frac{dP}{dx} = 100 12\sqrt{x}$  If the firm employs 25 more workers, them the new level production of items is:

**4.** Given vectors

 $\vec{p} = (a+1)\hat{i} + a\hat{j} + a\hat{k}$   $\vec{q} = a\hat{i} + (a+1)\hat{j} + a\hat{k}$   $\vec{r} = a\hat{i} + a\hat{j} + (a+1)\hat{k}$ are coplanar and 3( $\vec{p}.\vec{q}$ )<sup>2</sup> -  $\lambda |\vec{r} \times \vec{q}|^2 = 0$ then  $\lambda =$ 

- 5. Numbers of complex numbers satisfying |z| = 1 and  $\left|\frac{z}{\overline{z}} + \frac{\overline{z}}{z}\right| = 1$  is
- 6. The number of solutions of system of equations  $2 \sin^2 x + \sin^2 2x = 2\sin 2x$  $+ \cos 2x = \tan x$  in  $[0, 4\pi]$  satisfying  $2 \cos^2 x + \sin x \le 2$  is

7. 
$$\lim_{x \to \frac{\pi}{2}} \frac{\sin x - (\sin x)^{\sin x}}{1 - \sin x + \ln(\sin x)}$$
 is equal to

8. Let a = 8 and b = 3<sup>9</sup> and we define a sequence {u<sub>n</sub>} as follows u<sub>1</sub> = b,  $u_{n + 1} = \begin{cases} \frac{1}{3}u_{n}; & \text{if } u_{n} \text{ is multiple of } 3\\ u_{n} + a; & \text{otherwise} \end{cases}$ then

#### $u_{500}$ – $u_{300}$ – $u_{400}$ is equal to

9. Let  $A = [a_{ij}]_{3 \times 3}$ ,  $B = [b_{ij}]_{3 \times 3}$  where  $b_{ij} = 3^{i - j}a_{ij}$  and  $C = [c_{ij}]_{3 \times 3}$ , where  $c_{ij} = 4^{i - j}b_{ij}$  be any three matrices. If det. A = 2, then det. B + det. C is equal to

#### (SPACE FOR ROUGH WORK)

**10.** If  $\sqrt{a} + \sqrt{d} = \sqrt{c} + \sqrt{b}$  and ad = bc, where  $a,b,c,d \in R^+$  then the family of lines  $(a^2x+b^2y+c^2)+d^2x=0$  passes through a fixed point M(x<sub>0</sub>,y<sub>0</sub>). Find the value of  $(x_0^{-1}+y_0^{-1}) + 1$ 

#### (SPACE FOR ROUGH WORK)

#### PART - II [PHYSICS]

#### SAMPLE PAPER – JEE MAIN

#### SECTION - A [STRAIGHT OBJECTIVE TYPE]

**Q.1** to **Q.20** has four choices (A), (B), (C), (D) out of which **ONLY ONE** is correct

**1.** A particle of mass  $m_1$  is moving with a velocity  $v_1$  and another particle of mass  $m_2$  is moving with a velocity  $v_2$ . Both of them have the same momentum but their different kinetic energies are  $E_1$  and  $E_2$  respectively. If  $m_1 > m_2$  then :

(A) 
$$E_1 < E_2$$
 (B)  $\frac{E_1}{E_2} = \frac{m_1}{m_2}$   
(C)  $E_1 > E_2$  (D)  $E_1 = E_2$ 

**2.** A network of four capacitors of capacity equal to  $C_1=C$ ,  $C_2=2C$ ,  $C_3=3C$  and  $C_4=4C$  are connected to a battery as shown in the figure. The ratio of the charges on  $C_2$  and  $C_4$  is



**3.** The moment of inertia of a uniform circular disc of radius 'R' and mass 'M' about an axis passing from the edge of the disc and normal to the disc is-

(A) 
$$\frac{1}{2}$$
 MR<sup>2</sup>  
(B)  $\frac{7}{2}$  MR<sup>2</sup>  
(C)  $\frac{3}{2}$  MR<sup>2</sup>  
(D) MR<sup>2</sup>

- 4. A parallel plate air capacitor is charged to a potential difference of V volts. After disconnecting the charging battery the distance between the plates of the capacitor is increased using an insulating handle. As a result the potential difference between the plates :-
  - (A) Decreases
  - (B) Does not change
  - (C) Becomes zero
  - (D) Increases
- 5. Two bodies have their moments of inertia I and 2I resepctively about their axis of rotation. If their kinetic energies of rotation are equal, their angular momenta will be in the ratio-

(A) 1 : 2 (B) 
$$\sqrt{2}$$
 : 1  
(C) 1 :  $\sqrt{2}$  (D) 2 : 1

(SPACE FOR ROUGH WORK)

- 6. If dipole moment the magnetic of an atom of diamagnetic material, paramagnetic material and ferromagnetic material are denoted by  $\mu_{d},\,\mu_{p}$  and  $\mu_{f}$  respectively, then :-(A)  $\mu_p = 0$  and  $\mu_f \neq 0$ (B)  $\mu_d \neq 0$  and  $\mu_p = 0$ (C)  $\mu_d \neq 0$  and  $\mu_f \neq 0$ (D)  $\mu_d = 0$  and  $\mu_p \neq 0$
- 7. An electron moves in a circular orbit with a uniform speed v. It produces a magnetic field B at the centre of the circle. The radius of the circle is proportional to

(A) 
$$\sqrt{\frac{v}{B}}$$
 (B)  $\frac{v}{B}$   
(C)  $\frac{B}{v}$  (D)  $\sqrt{\frac{B}{v}}$ 

8. As a result of change in the magnetic flux linked to the closed loop shown in the figure, an e.m.f. V volt is induced in the loop. The work done (joules) in taking a charge Q coulomb once along the loop is :-



- 9. A particle executing simple harmonic motion of amplitude 5 cm has maximum speed of 31.4 cm/s. The frequency of oscillation is :
  (A) 1 Hz
  (B) 3 Hz
  (C) 2 Hz
  (D) 4 Hz
- **10.** In a circuit L, C and R are connected in series with an alternating voltage source of frequency f. The current leads the voltage by 45°. The value of C is-

(A) 
$$\frac{1}{2\pi f(2\pi fL - R)}$$
 (B)  $\frac{1}{2\pi f(2\pi fL + R)}$   
(C)  $\frac{1}{\pi f(2\pi fL - R)}$  (D)  $\frac{1}{\pi f(2\pi fL + R)}$ 

- **11.** A wave in a string has an amplitude of 2cm. The wave travels in the +ve direction of x-axis with a speed of 128 m/sec and it is noted that 5 complete waves fit in 4m length of the string. The equation describing the wave is-(A)  $y = (0.02)m \sin(7.85x - 1005t)$ (B)  $y = (0.02)m \sin(7.85x + 1005t)$ (C)  $y = (0.02)m \sin(15.7x - 2010t)$ (D)  $y = (0.02)m \sin(15.7x + 2010t)$
- 12. The pressure exerted by an electromagnetic wave of intensity I (Wm<sup>-2</sup>) on a non-reflecting surface is (c is the velocity of light)
  (A) Ic
  (B) Ic<sup>2</sup>
  (C) I/c
  (D) I/c<sup>2</sup>

(SPACE FOR ROUGH WORK)

- 13. Which one of the following statements is true-(A) Both light and sound waves in air are transverse (B) The sound waves in air are longitudinal while the light waves are transverse (C) Both light and sound waves in air are longitudinal (D) Both light and sound waves can travel in vacuum 14. The work functions for metals A, B and C are respectively 1.92 eV, 2.0 eV and 5eV. According to Einstein's equation, the metals which will emit photo electrons for a radiation of wavelength 4100Å is/are :-(A) None (B) A only (C) A and B only (D) All the three metals 15. A quantity y is related to another quantity x by the equation  $y = kx^a$ where k and a are constant. If percentage error in the measurement of x is p, then error in y depends upon
  - (A) k and a(B) x and a(C) p and a(D) p, k and a all

- **16.** An electron and proton are accelerated through same potential, then  $\lambda_e/\lambda_p$  will be (A) 1 (B)  $m_e/m_p$  (C)  $m_p/m_e$  (D)  $\sqrt{m_P/m_e}$
- An ideal gas heat engine operater in carnot cycle between 227°C and 127°C. It absorbs 6 × 10<sup>4</sup> cals of heat at higher temperature Amount of heat converted to work is.
  - (A)  $2.4 \times 10^4$  cals (B)  $6 \times 10^4$  cals (C)  $1.2 \times 10^4$  cals (D)  $4.8 \times 10^4$  cals
- **18.** The nuclei of which one of the following pairs of nuclei are isotones :-(A)  $_{34}Se^{74}$ ,  $_{31}Ga^{71}$  (B)  $_{38}Sr^{84}$ ,  $_{38}Sr^{86}$  (C)  $_{42}Mo^{92}$ ,  $_{40}Zr^{92}$  (D)  $_{20}Ca^{40}$ ,  $_{16}S^{32}$
- **19.** The molar specific heat at constant pressure of an ideal gas is (7/2)R. The ratio of specific heat at constant pressure to that at constant volume is-
  - (A)  $\frac{7}{5}$  (B)  $\frac{8}{7}$ (C)  $\frac{5}{7}$  (D)  $\frac{9}{7}$

#### (SPACE FOR ROUGH WORK)

**20.** Energy levels A, B and C of a certain atom correspond to increasing values of energy i.e.  $E_A < E_B < E_C$ . If  $\lambda_1, \lambda_2$  are  $\lambda_3$  wave lengths of radiations corresponding to transitions C to B, B to A and C to A respetively, which of the following relaitons is correct ?

(A)  $\lambda_1, \lambda_2 + \lambda_3$  (B)  $\lambda_1 + \lambda_2 + \lambda_3 = 0$ (C)  $\lambda_3^2 = \lambda_1^2 + \lambda_2^2$  (D)  $\lambda_3 = \frac{\lambda_1 \lambda_2}{\lambda_1 + \lambda_2}$ 

#### SECTION – B [NUMERICAL VALUE TYPE]

*Q.1* to *Q.10* are NUMERIC VALUE TYPE Questions. Candidates have to attempt any 5 Ques. out of 10.

- 1. A body is projected horizontally near the surface of the earth with  $\sqrt{1.5}$  times the orbital velocity. The maximum height up to which it will rise above the surface of the earth is 'n' times the radius of earth. Fill 'n' is OMR Sheet.
- 2. The magnetic field of a beam emerging from a filter facing a floodlight is given by  $B_0 = 12 \times 10^{-8} \sin (1.20 \times 10^7 z)$  $- 3.60 \times 10^{15} t) T.$

What is the average intensity of the beam ?

3. A small meteor approaches a planet on a hyperbolic path as shown. When it is at a large distance, it has a velocity  $v_{\infty}$ and impact parameter b = 8000 km. The escape speed from the planet is 6 km/s. What should be  $v_{\infty}$  (in km/s) so that the meteor just grazes the planet. The radius of planet is 6400 km.



A 1 KW signal is transmitted using a communication channel which provides attenuation at the rate of -2dB per km. If the communication channel has a total length of 5 km, the power (in W) of the signal received is

[gain in dB = 10 log  $\left(\frac{P_0}{P_1}\right)$ ]

#### (SPACE FOR ROUGH WORK)

5. Germanium and silicon junction diodes are connected in parallel. These are connected in series with a resistance R, a milliammeter (mA) and a key (K) as shown in fig. When key (K) is closed a current begins to flow in the milliammeter. The potential drop (in volt) across the germanium diode is



- 6. What is the maximum height (in m) of a brick column of uniform cross section for which column deformation due to its own weight is within the elastic limit?  $[P_{atmospheric} = 100 \text{ kPa}, \quad \rho = 1.8 \times 10^3 \text{ kg/m}^3. \text{ Elastic limit}, \sigma = 3.7 \text{ M Pa}.]$
- 7. Two identical plane mirrors are separated by  $60^{\circ}$ , as the drawing illustrates. If a ray strikes mirror  $M_1$  at its midpoint parallel to  $M_2$ , how many total reflections will occur from both mirrors put together.



- 8. N<sup>th</sup> level of Li<sup>2+</sup> has the same energy as the ground state energy of the hydrogen atom. If  $r_N$  and  $r_1$  is the radii of the N<sup>th</sup> Bohr orbit of Li<sup>2+</sup> and H atom respectively, then the ratio  $r_N/r_1$  is
- 9. Deuterium ions (deuterons) are accelerated to an energy of 2.0 MeV, and they strike a tritium target. As a result of the collision, fusion reaction occurs. Determine the kinetic energy (in MeV) of neutrons emitted perpendicular to the beam of incident deuterons. The fusion reaction is accompanied by the emission of one neutron. Approximate your answer to the nearest integer. For Q value, Take :  $m_D$  = 2.014 amu,  $m_T$  =  $3.016 \text{ amu}, \text{ m}_{\text{He}} = 4.002 \text{ amu}, \text{ m}_{\text{n}} =$ 1.008 amu. Take 1 amu = 900 MeV.
- **10.** A motorboat covers a given distance in 6 hr moving downstream on a river. It covers the same distance in 10 hr moving upstream. If the time it takes to cover the same distance in still water is

t, then write 
$$\frac{t}{2.5}$$
 in hrs.

(SPACE FOR ROUGH WORK)

#### PART - III [CHEMISTRY]

#### SAMPLE PAPER – JEE MAIN



**Q.1** to **Q.20** has four choices (A), (B), (C), (D) out of which **ONLY ONE** is correct

**1.** For the reaction,  $AB_2(g) + A(s) \rightleftharpoons B_2(g) + A_2(g)$ , following graph is obtained

# 

- where  $K \rightarrow Equilibrium$  Constant
- $T \rightarrow Temperature \ in \ Kelvin$  Which of the following will increase the concentration of  $AB_2$  at equilibrium.
- (A) Adding more of A (s)
- (B) Decreasing temperature
- (C) Adding inert gas at constant volume
- (D) Increasing the volume of container

- 2. The degree of hydrolysis of 0.1 M NaCN solution is 4%. What will be the solubility of Al(OH)<sub>3</sub> in this solution.  $[K_{sp Al(OH)_3} = 6.4 \times 10^{-20}]$ (A) 0.04 mol L<sup>-1</sup> (B) 10<sup>-15</sup> mol L<sup>-1</sup> (C) 10<sup>-12</sup> mol L<sup>-1</sup> (D) 1.6 × 10<sup>-7</sup> mol L<sup>-1</sup>
- 3. Surfactant molecules can cluster together as micelles, which are colloid sized cluster of molecules. Micelles form only above critical micelle concentration (CMC) and above certain temperature called Kraft temperature. ΔH of micelle formation can be positive or negative. Which of the following is NOT TRUE about micelle formation?
  - (A)  $\Delta S$  of micelle formation is positive

(B) the hydrophobic part lie towards interior of micelle

(C) the hydrophilic part lie towards surface of micelle

(D)  $\Delta S$  of micelle formation is negative

#### (SPACE FOR ROUGH WORK)



- When heated above 916°C, iron changes its bcc crystalline form to fcc without the change in the radius of atom. The ratio of density of the crystal before heating and after heating is :

  (A) 1.069
  (B) 0.918
  (C) 0.725
  (D) 1.231
- **8.** Which of the following metal nitrate can show given change.

Aqueous solution of metal nitrate NH<sub>4</sub>OH (No change in colour and no precipitate in test tube) (A) Pb(NO<sub>3</sub>)<sub>2</sub> (B) Fe(NO<sub>3</sub>)<sub>2</sub> (C) AqNO<sub>3</sub> (D) Hq(NO<sub>3</sub>)<sub>2</sub>

- **9.** When sodium is gradually added to liquid  $NH_3$  then which of the following property do not change ?
  - (A) Magnetic moment
  - (B) Electrical Conductivity
  - (C) Colour
  - (D) Oxidation state of Nitrogen
- 10. Which of the following would not give disproportionation reaction on hydrolysis?
  (A) KO<sub>2</sub>
  (B) N<sub>2</sub>O<sub>5</sub>
  (C) XeF<sub>4</sub>
  (D) K<sub>2</sub>O<sub>2</sub>

#### (SPACE FOR ROUGH WORK)

- 11. If number of monovalent oxygen and number of divalent oxygen per tetrahedral unit of silicate are equal then the silicate can be : (A) Soro silicate (B) Neso silicate (C) Pyroxene (D) Sheet silicate For carbonates of alkali metals as we 12. move down the group what will be the correct order of covalent characters, solubility and thermal stability -(A) Increase, Decrease, Increase (B) Decrease, Increase, Increase (C) Increase, Increase, Decrease (D) Decrease, Decrease, Increase 13. Select correct order of stability of following oxides. (A)  $CI_2O > Br_2O > I_2O$ (B)  $CI_2O > I_2O > Br_2O$ (C)  $I_2O > CI_2O > Br_2O$ (D)  $I_2O > Br_2O > Cl_2O$ Which of the following properties does 14. not belong to the complex formed in Mond's process. (A) It is diamagnetic
  - (B) It follows 18 electron rule
  - (C) It is square planar
  - (D) Volatile at 100°C

15. The best yield of given product can be obtained by using which set of reactants X and Y respectively

$$X + Y \xrightarrow{\text{Ether}} \langle DH_2 - CH_2 - CH_3 \rangle$$

- (A) PhLi + Neopentyl chloride
- (B) PhMgBr + Neopentyl bromide
- (C) t-Bu-MgBr + Benzyl bromide
- (D) Benzylchloride + t-Butyl chloride  $\xrightarrow{Na}$
- 16. Which of the following isomers having molecular formula C<sub>2</sub>H<sub>2</sub>Br<sub>2</sub> has highest dipole moment and boiling point but lowest melting point ?



(D) Not applicable to any single isomer

#### (SPACE FOR ROUGH WORK)



#### (SPACE FOR ROUGH WORK)

#### **SECTION - B**

#### [NUMERICAL VALUE TYPE]

**Q.21** to **Q.25** are **NUMERIC VALUE TYPE** *Questions.* 

- 1. Consider the following cell  $Pt | H_2(P_1atm) | H^+ (M_1) | | H^+ (M_2) | H_2$  $(P_2 atm) | Pt$ Where  $P_1$  and  $P_2$  are pressures.  $M_1$  and M<sub>2</sub> are molarities. What will be the emf of cell at  $25^{\circ}$ C if P<sub>1</sub> =  $P_2$  and  $M_1$  is 50% higher than  $M_2$ ? Repeat the magnitude of emf by multiplying with 10000. [Take :  $\frac{2.303 \text{ RT}}{\text{F}} = 0.06$  and log 3 = 0.48,  $\log 2 = 0.3$ ] 2. An unknown compound A dissociates at 500°C to give products as follows - $A(g) \rightleftharpoons B(g) + C(g) + D(g)$ Vapour density of the equilibrium mixture is 60 when it dissociates to the extent to 20%. What will be the molecular weight of Compound A -
- **3.** At 500 kilobar pressure density of diamond and graphite are 3 g/cc and 2 g/cc respectively, at certain temperature 'T'. Find the value of  $|\Delta H \Delta U|$  (kJ /mole) for the conversion of 1 mole of graphite to 1 mole of diamond at temperature 'T'.
- **4.** The following sequence of reaction occurs in commercial production of aqueous nitric acid.

 $\begin{array}{ll} 4\mathsf{NH}_3(g)+5\mathsf{O}_2(g) & \to 4\mathsf{NO}(g)+6\mathsf{H}_2\mathsf{O}(\mathsf{I}) & \Delta\mathsf{H}=-904\mathsf{kJ} & \dots(1) \\ 2\mathsf{NO}(g)+\mathsf{O}_2(g) & \to 2\mathsf{NO}_2(g) & \Delta\mathsf{H}=-112\mathsf{kJ} & \dots(2) \end{array}$ 

 $3NO_2(g) + H_2O(I) \longrightarrow 2HNO_3(aq) + NO(g) \quad \Delta H = -140kJ \dots(3)$ Determine the total heat (in kJ/mole) liberated at constant pressure for the production of exactly 1 mole of aqueous nitric acid by this process.

- **5.** How many P–O–P bonds are present in  $P_4O_{10}$ ?
- 6. Give the total number of possible structural isomers of the compound <sup>II</sup> [Cu(NH<sub>3</sub>)<sub>4</sub>[PtI<sub>4</sub>].
- Find the number of native ores out of given ores.
   Pyrolusite, Chromite, Siderite, Cassiterite, Calamine, Argentite, Lime stone, Chalcopyrite.

#### (SPACE FOR ROUGH WORK)



#### (SPACE FOR ROUGH WORK)

# MOTION

## **HINT & SOLUTION**

## **SAMPLE PAPER – JEE MAIN**

Duration: 3 Hours

Max. Marks : 300

#### PART - I [MATHEMATICS]

SECTION : A											
1	2	3	4	5	6	7	8	9	10		
С	В	А	В	А	В	В	С	С	С		
11	12	13	14	15	16	17	18	19	20		
Α	С	В	А	D	D	А	В	D	Α		
SECTION : B											
1	2	3	4	5	6	7	8	9	10		
2	36	3500	1	8	8	2	5	4	1		

#### PART - II [PHYSICS]

SECTION : A									
1	2	3	4	5	6	7	8	9	10
А	С	С	D	В	D	А	Α	А	В
11	12	13	14	15	16	17	18	19	20
А	С	В	С	D	D	С	А	А	D
SECTION : B									
1	2	3	4	5	6	7	8	9	10
2	1.71	8	100	0.7	200	2	3	15	3

#### PART - III [CHEMISTRY]

SECTION : A										
1	2	3	4	5	6	7	8	9	10	
В	С	D	В	Α	С	В	С	D	В	
11	12	13	14	15	16	17	18	19	20	
В	В	С	С	С	С	Α	В	Α	D	
SECTION : B										
21	22	23	24	25	26	27	28	29	30	
108	168	100	493	6	4	0	5	44	6	

#### PART - I [MATHEMATICS]

#### **SECTION - A**

#### 1. C

7 letters P  $\rightarrow$ E  $\rightarrow$ R  $\rightarrow$ F  $\rightarrow$ C  $\rightarrow$ T  $\rightarrow$ 2 alike + 2 diff. 1 ×  ${}^{5}C_{2} = 10$ All 4 different =  ${}^{6}C_{4} = 15 \Rightarrow 25$ 

#### 2.

В



#### 3.

Α

~[pv(~pvq)Demorgen's ~ $p\Lambda ~ (pvq)$ ~ $p\Lambda (p\Lambda ~q)$ 

**4. B**  $(I-A)^{-1} = I + A + A^2 + A^3 + \dots = I + A$  $+ A^2$ 

#### 5. A

#### 6. B

\*  $\rightarrow$  Any Head or tail ; P(H) = P(T) =  $\frac{1}{2}$  ,

P(\*) = 1 for at least four consecutive heads, we havefollowingpatterns

(i) HHHH\*\*\*]

(ii) THHHH\*\*  
(iii) \*THHHH\* 
$$\Rightarrow \left(\frac{1}{2}\right)^4 1 + 3\left(\frac{1}{2}\right)^5 \Rightarrow \frac{5}{32}$$

#### 7. B

 $\begin{array}{l} \mathsf{D}_1=\mathsf{p}^2-12\mathsf{q},\ \mathsf{D}_2=\mathsf{r}^2+4\mathsf{q};\ \mathsf{D}_3=\mathsf{s}^2-8\mathsf{q}\\ \textbf{Case I}-\mathsf{If}\ \mathsf{q}<0\ \mathsf{then}\ \mathsf{D}_1>0,\ \mathsf{D}_3>0\ \mathsf{and}\ \mathsf{D}_2\\ \mathsf{may}\ \mathsf{or}\ \mathsf{may}\ \mathsf{not}\ \mathsf{be}+\mathsf{ve}\\ \textbf{Case II}-\mathsf{If}\ \mathsf{q}>0\ \mathsf{then}\ \mathsf{D}_2\ >0\ \mathsf{and}\ \mathsf{D}_1,\ \mathsf{D}_3\\ \mathsf{may}\ \mathsf{or}\ \mathsf{may}\ \mathsf{not}\ \mathsf{be}+\mathsf{ve}\\ \textbf{Case III}-\mathsf{If}\ \mathsf{q}=0\ \mathsf{then}\ \mathsf{D}_1,\ \mathsf{D}_2,\ \mathsf{D}_3\geq 0\\ \mathsf{so},\ \mathsf{given}\ \mathsf{equation}\ \mathsf{has}\ \mathsf{at}\ \mathsf{least}\ \mathsf{two}\ \mathsf{real}\\ \mathsf{roots} \end{array}$ 

8.

С

С

С

$$(\tan^{-1}x - 2) \left( \cot^{-1}x - 1 - \frac{\pi}{2} \right) > 0$$
  
$$\Rightarrow (\tan^{-1}x + 1)(\tan^{-1}x - 2) < 0$$
  
$$\Rightarrow -1 < \tan^{-1}x < 2$$
  
$$\Rightarrow -\tan 1 < x < \tan 2$$

#### 9.

$$\begin{split} |w| &= 1 \Rightarrow |z - (1/5)i| = |z| \\ \Rightarrow |z - (1/5)i|^2 &= |z|^2 \\ \Rightarrow |x + iy - 1/5i]^2 &= |x + iy|^2 \\ \Rightarrow x^2 + (y - 1/5)^2 &= x^2 + y^2 \\ \Rightarrow -2/5y + 1/25 &= 0 \\ \Rightarrow 10y &= 1, \text{ which is a line }. \end{split}$$

10.

$$(x + \sqrt{x^3 - 1})^5 + (x - \sqrt{x^3 - 1})^5$$

=  $2[x^5 + 5C_2 \cdot x^3 (x^3 - 1) + 5C_4 x(x^3 - 1)^2]$ =  $2[x^5 + 10x^3 (x^3 - 1) + 5x(x^6 - 2x^3 + 1)]$ =  $10x^7 + 20x^6 + 2x^5 - 20x^4 - 20x^3 + 10x$ ∴ polynomial has order of 7.

$$f(x) = \begin{vmatrix} x^2 + 3x & x - 1 & x - 3 \\ x + 1 & 2 - x & x - 3 \\ x - 3 & x + 4 & 3x \end{vmatrix}$$

$$f'(0) = \begin{vmatrix} 3 & -1 & -3 \\ 1 & 2 & -3 \\ 1 & 4 & 0 \end{vmatrix} + \begin{vmatrix} 0 & 1 & -3 \\ 1 & -1 & -3 \\ -3 & 1 & 0 \end{vmatrix} + \begin{vmatrix} 0 & -1 & 1 \\ 1 & 2 & 1 \\ -3 & 4 & 3 \end{vmatrix}$$

$$= 36 + 3 - 6 + 9 + 6 + 6 + 10 = 64$$

Α

$$S = \lim_{n \to \infty} \left\{ \frac{1}{(n+1)(n+2)} + \frac{1}{(n+2)(n+4)} + \frac{1}{(n+2)(n+4)} + \frac{1}{(n+n)(n+2n)} \right\}$$
$$= \lim_{n \to \infty} \sum_{r=1}^{n} \frac{n^{2}}{(n+r)(n+2r)} \cdot \frac{1}{n}$$
$$= \lim_{n \to \infty} \sum_{r=1}^{n} \frac{1}{\left(1 + \frac{r}{n}\right) \left(1 + \frac{2r}{n}\right)} \cdot \frac{1}{n} \frac{r}{n} \to x, \frac{1}{n} \to dx$$
$$a = \lim_{n \to \infty} (r / n)_{r=1} = 0, b = \lim_{n \to \infty} \left(\frac{r}{n}\right)_{r=n} = 1$$
$$\Rightarrow \qquad S \qquad = \int_{0}^{1} \frac{dx}{(1+x)(1+2x)} = \int_{0}^{1} \left(\frac{2}{1+2x} - \frac{1}{1+x}\right) dx$$
$$= \left[\log(1+2x) - \log(1+x)\right]_{0}^{1} = \log(3 / 2)$$

D  
Given loop is  

$$4y^2 = x^2 (4 - x^2)$$
  
Required area  $= \frac{4}{2} \int_0^2 x \sqrt{4 - x^2} dx$   
 $= \begin{bmatrix} 4 - x^2 = t^2 \\ xdx = -tdt \end{bmatrix}$   
 $= -2 \int_2^0 t tdt = -2 \left(\frac{t^3}{3}\right)_2^0$   
 $= -\frac{2}{3} \left(0 - 8\right) = \frac{16}{3} \operatorname{sq.}$  unit

#### 16. D

$$\frac{xdy - ydx}{x^2} = \sqrt{1 - \left(\frac{y}{x}\right)^2} \cdot \frac{dx}{x}$$
$$\frac{d\left(\frac{1}{x}\right)}{\sqrt{1 - \left(\frac{y}{x}\right)^2}} = \left(\frac{dx}{x}\right) \Rightarrow \sin^{-1}\left(\frac{y}{x}\right) = \log x + C$$
$$x = 1, y = 0$$
$$\Rightarrow C = 0$$
$$y = xsin(\log x)$$

#### 17.

Α

 $\begin{aligned} &(z^n-1) = (z-\alpha_0) \; (z-\alpha_1) \; ...... \; (z-\alpha_{n-1}) \\ &/n \; (z^n-1) = /n \; (z-\alpha_0) + /n \; (z-\alpha_1) \; ..... \\ &+ /n \; (z-\alpha_{n-1}) \end{aligned}$ 

$$\frac{n \cdot z^{n-1}}{z^n - 1} = \sum_{r=0}^{n-1} \frac{1}{z - \alpha_r} \implies \frac{n \cdot 3^{n-1}}{3^n - 1}$$
  
=  $\sum_{r=0}^{n-1} \frac{1}{3^n - \alpha_r}$   
Now,  $\sum_{r=0}^{n-1} \frac{\alpha_r}{3 - \alpha_r} = \sum_{r=0}^{n-1} \left(\frac{3}{3 - \alpha_r} - 1\right) =$   
 $\frac{n \cdot 3^n}{3^n - 1} - n = \frac{n}{3^n - 1}$ 

18.

В

By sine rule  

$$\frac{\sin 30^{\circ}}{\ell} = \frac{\sin 45^{\circ}}{\left(\sqrt{3}+1\right)}$$

$$\Rightarrow \ell = \frac{\sqrt{3}+1}{\sqrt{2}} = \frac{\sqrt{2}}{\sqrt{3}-1}$$

#### 19. D

 $\begin{vmatrix} \alpha & 1 & 3 \\ 2 & 1 & -4 \\ \alpha & -2 & 3 \end{vmatrix} = 0$  $\Rightarrow 3\alpha^{2} + 18 = 0$  $\Rightarrow a \in \phi$ 

#### 20.

Α

Perpendicular vector to the plane  $\vec{n} = \begin{vmatrix} i & j & k \\ 1 & 2 & -1 \\ -1 & 1 & -2 \end{vmatrix} = -3\hat{i} + 3\hat{j} + 3\hat{k}$ Eq. of plane -3(x-1)+3(y-1)+3z = 0  $\Rightarrow x - y - z = 0$  $d_{(2,1,4)} = \frac{|2-1-4|}{\sqrt{1^2 + 1^2 + 1^2}} = \sqrt{3}$ 

#### **SECTION - B**

1.

 $3,1,1, \& 2,2,1 \rightarrow \text{two methods only}$ 

- 2. 36
- 3. 3500

2

4. **1**  $\vec{p}, \vec{q}, \vec{r}$  being coplanar  $[\vec{p} \vec{q} \vec{r}] = 0$ 

$$\begin{vmatrix} a+1 & a & a \\ a & a+1 & a \\ a & a & a+1 \end{vmatrix} = 0$$
  
$$\Rightarrow a = -\frac{1}{3}$$
  
$$3(\vec{p} \cdot \vec{q})^2 = \lambda |\vec{r} \times \vec{q}|^2$$
  
$$3\left(\frac{1}{9}\right) = \lambda\left(\frac{1}{3}\right)$$
  
$$\lambda = 1$$

#### 5.

8

Let  $z = \cos\theta + i\sin\theta$ ,  $\theta \in [0,2p)$  then  $\left|\frac{z}{\overline{z}} + \frac{\overline{z}}{z}\right| = 1 \Rightarrow \left|\frac{z^2 - \overline{z}^2}{|z|^2}\right| = 1$   $\Rightarrow 2|\cos 2\theta| = 1 \Rightarrow \cos 2\theta = \frac{1}{2} \text{ or } \frac{1}{2}$   $\therefore$  Number of values of  $\theta = 8$   $\therefore$  Number of values of z = 88

#### 6.

 $\begin{array}{l} 2\,\sin^2 x\,+\,\sin^2 2x\,=\,2\\ \Rightarrow\,2\,\sin^4 x\,-\,3\,\sin^2 x\,+\,1\,=\,0\\ \Rightarrow\,(2\,\sin^2 x\,-\,1)\,(\sin^2 x\,-\,1)\,=\,0\,\ldots.(A)\\ \text{Also}\,\sin\,2x\,+\,\cos\,2x\,=\,\tan\,x\\ \Rightarrow\,(1\,+\,\tan\,x)\,(\tan^2 x\,-\,1)\,=\,0\,\ldots.(B)\\ 2\,\cos^2 x\,+\,\sin\,x\,\leq\,2\\ \Rightarrow\,\sin\,x\,(2\,\sin\,x\,-\,1)\,\geq\,0\\ \Rightarrow\,\sin\,x\,(2\,\sin\,x\,-\,1)\,\geq\,0\\ \Rightarrow\,\sin\,x\,\leq\,0\quad\text{or}\,\,\sin\,x\,\geq\,\frac{1}{2}\quad\ldots.(C)\\ \text{From (A), (B) & (C) get results} \end{array}$ 

#### 7.

2

Put sin x = 1 + t 
$$\Rightarrow$$
 if x  $\rightarrow \frac{\pi}{2}$   
 $\Rightarrow$  t  $\rightarrow 0^{-} \lim_{t \to 0^{-}} \frac{(1+t) - (1+t)^{(1+t)}}{-t + \ln(1+t)}$   
=  $\lim_{t \to 0^{-}} \frac{(1+t)^{t} - 1}{t - \ln(1+t)}$   
=  $\lim_{t \to 0^{-}} \frac{1+t^{2} + \frac{t(t+1)t^{2}}{2!} + \dots - 1}{t - \left(t - \frac{t^{2}}{2} + \frac{t^{3}}{3} + \dots - 1\right)} = 2.$ 

8.

5

 $\begin{array}{l} u_{10}=1=u_{13}\ =u_{16}\ \ldots \ =u_{3k\ +\ 1} \ \text{for} \ k\geq 3\\ u_{11}=9=u_{14}\ =u_{17}.\ldots \ =u_{3k\ +\ 2}\\ u_{12}=3=u_{15}\ =u_{18}\ \ldots \ =u_{3k}\\ u_{500}=9\\ u_{400}=1\\ u_{300}=3 \end{array}$ 

#### 9.

4

We have det. B = det. C = det.A = 2, because

det. B = 
$$\begin{vmatrix} a_{11} & \frac{a_{12}}{3} & \frac{a_{13}}{3^2} \\ 3a_{21} & a_{22} & \frac{1}{3}a_{23} \\ 9a_{31} & 3a_{32} & a_{33} \end{vmatrix}$$
 =  $|A| = 2$ 

Similarly det. C = det. B = |A| = 2Hence det. B + det. C = 2 + 2 = 4

#### 10.

1

We have a + d + 
$$2\sqrt{ad}$$
 = c + b +  $2\sqrt{bc}$   
 $\Rightarrow$  a + d = c + b (As ad = bc)  
 $\therefore$  a<sup>2</sup>+d<sup>2</sup>+2ad = c<sup>2</sup>+b<sup>2</sup>+2bc  
 $\Rightarrow$  a<sup>2</sup>+d<sup>2</sup>=c<sup>2</sup>+b<sup>2</sup>  
(a<sup>2</sup>+d<sup>2</sup>)x+b<sup>2</sup>y+c<sup>2</sup>=0  
 $\Rightarrow$  (b<sup>2</sup>+c<sup>2</sup>)x+b<sup>2</sup>y+c<sup>2</sup>=0  
 $\Rightarrow$  b<sup>2</sup>(y+x)+c<sup>2</sup>(x+1)=0  
(y +x) +  $\frac{c^2}{b^2}(x+1) = 0$   
Which is of the form L<sub>1</sub>+ $\lambda$ L<sub>2</sub>=0.

So, fixed point is  $(-1,1) = (x_0,y_0)$  (Given). Hence  $(x_0^{-1} + y_0^{-1}) = -1 + 1 = 0$ 

#### SECTION – A

A  

$$\therefore \text{ K.E} = \frac{p^2}{2m}$$
Given momentum is same  
and  $m_1 > m_2$   
 $E_1 = \frac{p^2}{2m_1} = m_2$ 

$$\frac{\frac{-1}{E_2}}{\frac{1}{E_2}} = \frac{\frac{2m_1}{p^2}}{\frac{p^2}{2m_2}} = \frac{m_2}{m_1}$$
  
So,  $E_1 < E_2$ 

2.

С

1.



Equivalent capacitance for three capacitors  $(C_1, C_2 \otimes C_3)$  in series is given by

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} = \frac{C_2C_3 + C_3C_1 + C_1C_2}{C_1C_2C_3}$$
  

$$\Rightarrow C_{eq.} = \frac{C_1C_2C_3}{C_1C_2 + C_2C_3 + C_3C_1}$$
  

$$\Rightarrow C_{eq.} = \frac{C(2C)(3C)}{C(2C) + (2C)(3C) + (3C)C} = \frac{6}{11}C$$
  

$$\Rightarrow Charge on capacitors (C_1, C_2 \& C_3) in$$

series  $6C_{11}$ 

$$= C_{eq.} V = \frac{22}{11} V$$

Charge on capacitor  $C_4 = C_4 V = 4CV$ 6C V

$$\frac{\text{ChargeonC}_2}{\text{ChargeonC}_4} = \frac{\overline{11}}{4\text{CV}} = \frac{6}{11} \times \frac{1}{4} = \frac{3}{22}$$

3.

С

By Parallel axis theorem  

$$I = I_{cm} + MR^{2}$$

$$I = \frac{MR^{2}}{2} + MR^{2}$$

$$I = \frac{3MR^{2}}{2}$$

#### 4. D

If we increase the distance between the plates its capacity decreases resulting in higher potential as we know Q = CV. Since Q is constant (bettery has been disconnected), on decreasing C, V will increase

#### 5. B

Given rotational KE are same

 $K.E. = \frac{1}{2} I\omega^{2}$   $I_{1}\omega_{1}^{2} = I_{2}\omega_{2}^{2}$   $I \omega_{1}^{2} = 2I \omega_{2}^{2}$   $\frac{\omega_{1}}{\omega_{2}} = \sqrt{2}$   $\frac{L_{1}}{L_{2}} = \frac{I_{1}\omega_{1}}{I_{2}\omega_{2}}$   $= \frac{I}{2I} \times \sqrt{2}$   $\frac{L_{1}}{L_{2}} = \frac{1}{\sqrt{2}}$ 

#### **6**.

 $\begin{matrix} \textbf{D} \\ \mu_d \ = \ 0 \ \& \ \mu_p \neq 0 \end{matrix}$ 

7.

Centripetal force is provided by magnetic  $F_{centripetal} = F_{magnetic}$ 

$$\therefore \frac{mv^2}{r} = 2vB$$
$$r = \frac{mv}{2B}$$
$$r \propto \frac{v}{B}$$

8.

А

Α

Work done due to a charge W = QV.

9.

$$v_{max} = A\omega 
\frac{31.4}{100} = 2\pi f \times \frac{5}{100} 
f = \frac{10}{10}, f = 1 Hz$$

#### 10. B

$$\tan \phi = \frac{X_c - X_L}{R}$$
$$\tan 45^\circ = \frac{\frac{1}{2\pi fc} - 2\pi fL}{R}$$
$$C = \frac{1}{2\pi f (2\pi fL + R)}$$

11. A

A = 2 cm,  $\frac{\omega}{k} = 128 \text{ms}^{-1}, 5\lambda = 4, \ \lambda = \frac{4}{5} \text{m}$ Y = A sin (kx- $\omega$ t) K =  $\frac{2\pi}{\lambda} = \frac{2\pi \times 5}{4} = \frac{31.4}{4} = 7.85$   $\therefore \omega = 128 \times 7.85 = 1005$ So, Y = 0.02m sin (7.85x-1005t)

#### 12.

С

We know =  $F = \frac{IA}{C}$ 

$$\mathsf{P} = \frac{\mathsf{F}}{\mathsf{A}} = \frac{\mathsf{I}_{\mathsf{A}/\mathsf{C}}}{\mathsf{A}} = \frac{\mathsf{I}}{\mathsf{C}}$$

#### 13. B

#### 14. C

Energy of electron with an associated wavelength of 4100  $\mbox{A}^{\rm o}$  is

$$\Rightarrow \frac{hc}{\lambda} = 4.85 \times 10^{-19} \text{J} = 3.024 \text{ ev}$$

This incident electron would emit photon from metals whose work potential is less than its energy.

Thus, it would emit photons from metal A and B

#### 15. D

$$y = kx^{a}$$
$$\frac{\Delta y}{y} = q \times \frac{\Delta x}{x} = a \times p$$

16. D

$$\lambda \propto \frac{1}{\sqrt{2mE}}$$
$$\lambda \propto \frac{1}{\sqrt{m}}$$
$$\frac{\lambda_{e}}{\lambda_{p}} = \sqrt{\frac{m_{p}}{m_{e}}}$$

17. C

$$\eta = \frac{W}{Q} = 1 - \frac{T_2}{T_1} \Rightarrow W = Q \left( 1 - \frac{T_2}{T_1} \right)$$
$$= 1.2 \times 10^4 \text{ cals}$$

18. A

By Theory

19. A

$$C_{p} = \frac{7}{2}R, C_{V} = C_{P} - R = \frac{7}{2}R - R = \frac{5}{2}R$$
$$\frac{C_{P}}{C_{V}} = \frac{(7/2)R}{(5/2)R} = \frac{7}{5}$$

20.

D

$$E_{c} = E_{B} = hc/\lambda_{1} \qquad -(1)$$

$$E_{B} = E_{A} = hc/\lambda_{2} \qquad -(2)$$

$$E_{c} - E_{A} = hc/\lambda_{3} \qquad -(3)$$

$$(1) + (2) - (3) = 0$$

$$\Rightarrow \frac{1}{\lambda_{1}} + \frac{1}{\lambda_{2}} = \frac{1}{\lambda_{3}} = \frac{\lambda_{1}\lambda_{2}}{\lambda_{1} + \lambda_{2}} = \lambda_{3}$$

**SECTION - B** 



 $R' \rightarrow Maximum height$ Apply momentum & energy conservation momentum conservation  $mv_0 R = mv'R' \qquad ...(i)$ 

$$-\frac{GMm}{R} + \frac{1}{2}mV_0^2$$

$$= -\frac{GMm}{R'} + \frac{1}{2}mv'^2 \qquad \dots (ii)$$
From eq<sup>n</sup> (i) & (ii)  
R' = 3R  
 $\Rightarrow R = h = 3R$ 

[ $\therefore$  h  $\rightarrow$  heigh from earth surface] h = 2R

8

$$\begin{split} I_{av} &= \frac{1}{2} \, c \, \frac{B_0^2}{\mu_0} \! = \! \frac{1}{2} \! \times \! \frac{3 \! \times \! 10^8 \times (12 \! \times \! 10^{-8})^2}{1.26 \! \times \! 10^{-6}} \\ &= 1.71 \ \text{w/m}^2 \end{split}$$

#### 3.

1.

L = const.  
mbV<sub>∞</sub> = mV<sub>1</sub> × R  

$$- \frac{GMm}{\infty} + \frac{1}{2}mV_{\infty}^{2}\left(\frac{b^{2}}{R^{2}} - 1\right)$$

$$V_{\infty} = \sqrt{\frac{2GM}{R}} \times \frac{R}{\sqrt{b^{2} - R^{2}}}$$

$$= 6 \times \frac{6400}{\sqrt{800^{2} - 6400^{2}}}$$

$$= 6 \times \frac{6400}{800\sqrt{100 - 64}}$$

$$= 8 \text{ km/s}$$

#### 4. 100

#### 5. 0.7

In fig. germanium diode is reverse biased and silicon diode is forward biased. Therefore, there will be no current in the branch of germanium diode. The potential barrier of silicon diode is 0.7V. Therefore, for conduction minimum potential difference across silicon is 0.7 V. Maximum potential difference across resistance, R = 12 - 0.7 = 11.3 V.

200  $P_0 + H\rho g = 3.7 \times 10^6$   $H \times 1.8 \times 10^3 \times 10 = 3.6 \times 10^6$  $H = \frac{36}{18} \times 10^2 = 200$ 

7. 2

6.

After two reflection, ray will become parallel to first mirror.

8. 3

9.

10.

**3**  $d = (v + u) 6 \qquad \dots(1)$   $d = (v - u) 10 \qquad \dots(2)$   $\left(\frac{v + u}{v - u}\right) \frac{6}{10} = 1$  v = 4u  $d = (5u) 6 \qquad \Rightarrow d = 30 u$  d = vt  $t = \frac{d}{v} = \frac{30u}{4u} = 7.5 \text{ hr}$ 

#### **SECTION - A**

Reaction is endothermic  $\Rightarrow \Delta H = \text{positive}$ So on increasing temperature reaction will shift forward. On decreasing volume concentration of every species will increases.

#### 2. C

1.

В

 $\begin{array}{ll} \text{CN}^{-} + \text{H}_2\text{O} \rightleftharpoons \text{HCN} + \text{OH}^{-} \\ \text{0.1-0.1 h} & \text{0.1 h} \\ [\text{OH}^{-}] = 0.1 \times 0.04 = 4 \times 10^{-3} \text{ M} \\ \text{K}_{\text{sp}} = [\text{AI}^{3+}] [\text{OH}^{-}]^3 \\ \text{6.4} \times 10^{-20} = \text{S} \times [4 \times 10^{-3}]^3 \\ \text{S} = 10^{-12} \text{ mol } \text{L}^{-1} \end{array}$ 

#### 3. D

The formation of micelle only above certain temperature called Kraft temperature suggests positive  $\Delta S$  of micelle formation which even overcome effect of positive  $\Delta H$  of micelle formation. Besides kinetic effect also become important at high temperature.

#### 4. B

5.

A  

$$\frac{mv^{2}}{r} = \frac{KZe^{2}}{r^{2}}$$
For H : Z = 1  

$$\frac{mv^{2}}{r} = \frac{Ke^{2}}{r^{2}} \left(K = \frac{1}{4}e^{2}\right)$$

$$\frac{mv^{2}}{r} = \frac{1}{4\pi\epsilon_{0}}\frac{e^{2}}{r^{2}}$$

$$v^{2} = \frac{e^{2}}{4\pi\epsilon_{0}rm}$$

$$v = \frac{e}{\sqrt{4\pi\epsilon_{0}rm}}$$

#### 6. C

$$\begin{array}{c} 2\text{CrO}_{4}^{2^{-}} \underbrace{H^{+}}_{OH^{-}} \text{Cr}_{2}\text{O}_{7}^{2^{-}} + \text{H}_{2}\text{O}\\ (d^{3}\text{s}, \\ \text{tetrahedral}) \end{array}$$

#### 7.

В

С

$$\frac{d_{_{bcc}}}{d_{_{fcc}}} = \frac{\left(2M \times 3\sqrt{3}/(N_{_A} \times 64r^3)\right)}{\left(4M \times 2\sqrt{2}/(N_{_A} \times 64r^3)\right)} = 0.918$$

#### 8.

(A)  $Pb(NO_3)_2$  (White)  $\xrightarrow{Excess}_{NH_4OH}$   $Pb(OH)_2 \downarrow$  (White) (B)  $Fe(NO_3)_2$  (White)  $\xrightarrow{Excess}_{NH_4OH}$   $Fe(OH)_2 \downarrow$  (Green) (C)  $AgNO_3$  (White)  $\xrightarrow{Excess}_{NH_4OH}$   $[Ag(NH_3)_2]^+$ (soluble complex) (D)  $Hg(NO_3)_2$  (White)  $\xrightarrow{Excess}_{NH_4OH}$   $HgO.HgNH_2NO_3 \downarrow$ 

### 9. D

 $Na + (x+y) NH_3(I) \rightarrow [Na^+(NH_3)_x] + [e^- (NH_3)_y]$ 

#### 10. B

(A) 
$$KO_{2}^{-1} + H_{2}O \longrightarrow KOH^{(+5)} + H_{2}O_{2}^{(-2)} + O_{2}^{(0)}$$
  
(B)  $N_{2}O_{5}^{+5} + H_{2}O \longrightarrow HNO_{3}^{(+5)}$   
(C)  $Xe^{+4}F_{4} + H_{2}O \rightarrow Xe^{-1} + Xe^{-1}O_{3} + HF + O_{2}$   
(D)  $K_{2}O_{2} + H_{2}O \longrightarrow RT \longrightarrow KOH + H_{2}O + O_{2}$ 

#### 11. B

No. of monovalent oxygen = no.of divalent oxygen = (2) Name : Pyroxene (single chain)

#### 12. B

Carbonates of alkali metals (a) Covalent character  $\rightarrow$  Li<sub>2</sub>CO<sub>3</sub> > Na<sub>2</sub>CO<sub>3</sub> > K<sub>2</sub>CO<sub>3</sub> > Rb<sub>2</sub>CO<sub>3</sub> > Cs<sub>2</sub>CO<sub>3</sub> (b) Solubility  $\rightarrow$  Li<sub>2</sub>CO<sub>3</sub> < Na<sub>2</sub>CO<sub>3</sub> < K<sub>2</sub>CO<sub>3</sub> < Rb<sub>2</sub>CO<sub>3</sub> < Cs<sub>2</sub>CO<sub>3</sub> (c) Thermal stability  $\rightarrow$  Li<sub>2</sub>CO<sub>3</sub> < Na<sub>2</sub>CO<sub>3</sub> < K<sub>2</sub>CO<sub>3</sub> < Rb<sub>2</sub>CO<sub>3</sub> < Cs<sub>2</sub>CO<sub>3</sub>

#### 13. C

Stability of halogen oxide :  $I_2O > Cl_2O > Br_2O$ 

14. C

Ni (s) + 4CO (g)  $\longrightarrow$  Ni(CO)<sub>4</sub>(g) d<sup>10</sup>, sp<sup>3</sup>, tetrahedral complex

15.



16.



Order of dipole moment = I > II > III. Boiling point depends on dipole moment while melting point depends on symmetry.

#### 17. A

Acids dissolves in NaHCO<sub>3</sub> but phenols are insoluble.



18. B



19.

20. D

#### SECTION – B

1. 108

Pt |  $H_2(P_1atm)$  |  $H^+$  ( $M_1$ ) | |  $H^+$  ( $M_2$ ) |  $H_2$ ( $P_2$  atm) | Pt

at anode 
$$H_2 \longrightarrow 2H^+ + 2e^-$$
  
 $P_1 \qquad (M_1)$   
at cathode  $2H^+ \longrightarrow H_2$   
 $(M_2) \qquad P_2$   
net  $2H^+ + H_2(P_1) \longrightarrow 2H^+ + H_2(P_2)$   
cell  $(M_2) \qquad (M_1)$   
reaction

$$\begin{split} \mathsf{E}_{\mathsf{Cell}} &= \ \mathsf{E}_{\mathsf{Cell}}^{\circ} - \frac{0.06}{2} \log \frac{[\mathsf{H}^+]^2(\mathsf{P}_2)}{(\mathsf{H}^+)^2(\mathsf{P}_1)} \ \because \ \mathsf{P}_1 = \mathsf{P}_2 \\ \mathsf{E}_{\mathsf{Cell}}^{\circ} &= 0 \\ \mathsf{E}_{\mathsf{Cell}} &= \ 0 \\ \mathsf{E}_{\mathsf{Cell}} &= \ -\frac{0.06}{2} \log \frac{[\mathsf{H}^+]_{\mathsf{M}_1}^2}{[\mathsf{H}^+]_{\mathsf{M}_2}^2} \\ &= \ -\frac{0.06}{2} \log (1.5)^2 = -0.0108 \mathsf{V} \end{split}$$

$$\begin{array}{l} \mathsf{A}(g) \rightleftharpoons \mathsf{B}(g) + \mathsf{C}(g) + \mathsf{D}(g) \\ \alpha = 0.2 \qquad \mathsf{VD} = 60 \\ \Rightarrow \mathsf{M}_{obs} = 120 \qquad \mathsf{n} = 3 - 1 = 2 \\ \alpha = \frac{\mathsf{M}_{\mathsf{Th}} - \mathsf{M}_{Obs}}{\mathsf{M}_{Obs}(\mathsf{n} - 1)} \\ 0.2 = \frac{\mathsf{M}_{\mathsf{Th}} - 120}{120(3 - 1)} \\ \mathsf{M}_{\mathsf{Th}} &= (0.2 \times 240) + 120 \\ &= 48 + 120 \\ &= 168 \; \mathsf{Ans.} \end{array}$$

#### 3. 100

C (graphite) 
$$\longrightarrow$$
 C (diamond)  
 $\Delta H = \Delta U + P_2 V_2 - P_1 V_1$   
 $\Delta H - \Delta U = (500 \times 10^3 \times 10^5 \text{ N/m}^2)$   
 $\left(\frac{12}{3} - \frac{12}{2}\right) \times 10^{-6}$   
 $= \frac{48}{35} \times 500 \times 10^2 \text{ J} = \frac{48}{7} \times 10^4 \text{ J}$   
 $= 500 \times 2 \times 10^3 \times 10^5 \times 10^{-6}$   
 $= 100 \text{ kJ /mole}$   
or 1000 bar  $\cdot$  litre mole<sup>-1</sup>]

#### 493 4.

1 mole of HNO<sub>3</sub> = 
$$\frac{3}{2}$$
 moles of NO<sub>2</sub>  $\longrightarrow$   
 $\frac{3}{2}$  mole of NO  $\longrightarrow \frac{3}{2}$  mole of NH<sub>3</sub>  
-  $\left(\frac{3}{2} \times \frac{1}{4}\right)(904) - \left(\frac{3}{2} \times \frac{1}{2}\right)(112) - \left(\frac{3}{2} \times \frac{1}{3}\right)(140)$   
= 493

5.

6



6.

4

0

(1) [Cu(NH<sub>3</sub>)<sub>4</sub>] [PtCl<sub>4</sub>] (2) [Cu(NH<sub>3</sub>)<sub>3</sub>Cl] [PtCl<sub>3</sub>(NH<sub>3</sub>)] (3) [Pt(NH<sub>3</sub>)<sub>3</sub>Cl] [CuCl<sub>3</sub>(NH<sub>3</sub>)] (4)  $[Pt(NH_3)_4] [CuCl_4]$ 

#### 7.

Native ore  $\Rightarrow$  An sedimentary rock that contains a metal element in it pure state. Pyrolusite  $\rightarrow$  MnO<sub>2</sub> Chromite  $\rightarrow$  FeCr<sub>2</sub>O<sub>4</sub> Siderite  $\rightarrow$  FeCO<sub>3</sub> Cassiterite  $\rightarrow$  SnO<sub>2</sub> Calamine  $\rightarrow$  ZnCO<sub>3</sub> Argentite  $\rightarrow Ag_2S$ Lime stone  $\rightarrow$  CaCO<sub>3</sub> Chalcopyrite  $\rightarrow$  CuFeS<sub>2</sub>

#### 8.

5

Because compound have 5  $\alpha$ -H-atom





10.